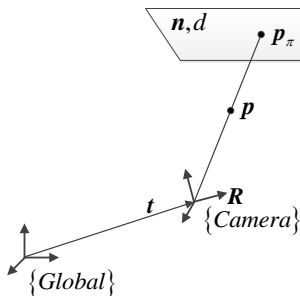


Shadow-SLAM

Sun Qinxuan

November 23, 2018

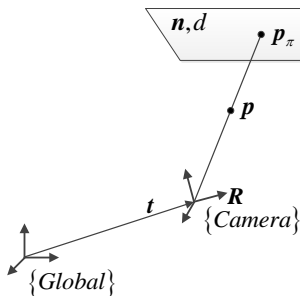
Occluded Point坐标计算



- 平面: n^T, d
- $\{Camera\}$ 坐标系到 $\{Global\}$ 坐标系的变换为 $\{R, t\}$
- $\{Camera\}$ 坐标系原点与occluding point p 确定的直线与该平面的交点坐标为

$$p_\pi = \frac{n^T t + d}{n^T (t - p)} p + \frac{n^T p + d}{n^T (p - t)} t \quad (1)$$

Occluded Point坐标计算



• p_π 在 $\{Camera\}$ 坐标系中的坐标为 $(R_{cg} = R^T, t_{cg} = -R^T t)$

$$\begin{aligned} {}^C p_\pi &= R_{cg} p_\pi + t_{cg} \\ &= \frac{n^T t + d}{n^T (p - t)} R^T (t - p) \end{aligned} \quad (2)$$

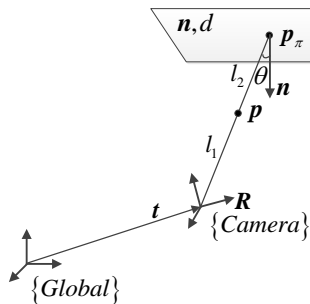
相机运动对Occluded point坐标的影响

- Jacobian of ${}^C\mathbf{p}_\pi$ w.r.t. $\{\mathbf{R}, \mathbf{t}\}$

$$\begin{aligned}\mathbf{J}_{p\pi} &= \frac{\partial {}^C\mathbf{p}_\pi}{\partial \xi} = \left[\frac{\partial {}^C\mathbf{p}_\pi}{\partial \mathbf{t}}, \frac{\partial {}^C\mathbf{p}_\pi}{\partial \omega} \right] \\ \frac{\partial {}^C\mathbf{p}_\pi}{\partial \mathbf{t}} &= \frac{\mathbf{n}^T \mathbf{p} + d}{(\mathbf{n}^T (\mathbf{p} - \mathbf{t}))^2} \mathbf{R}^T (\mathbf{t} - \mathbf{p}) \mathbf{n}^T + \frac{\mathbf{n}^T \mathbf{t} + d}{\mathbf{n}^T (\mathbf{p} - \mathbf{t})} \mathbf{R}^T \\ \frac{\partial {}^C\mathbf{p}_\pi}{\partial \omega} &= \frac{\mathbf{n}^T \mathbf{t} + d}{\mathbf{n}^T (\mathbf{p} - \mathbf{t})} \mathbf{R}^T [\mathbf{t} - \mathbf{p}]_\times\end{aligned}\quad (3)$$

where $[\mathbf{t} - \mathbf{p}]_\times$ is the skew-symmetric matrix corresponding to $\mathbf{t} - \mathbf{p}$.

相机运动对Occluded point坐标的影响



• 令 $l_1 = \|\mathbf{p} - \mathbf{t}\|_2$, $l_2 = \|\mathbf{p}_\pi - \mathbf{p}\|_2$,
 $l = l_1 + l_2 = \|\mathbf{p}_\pi - \mathbf{t}\|_2$, θ 角如图所示, 则有

$$\mathbf{n}^T(\mathbf{p} - \mathbf{t}) = -l_1 \cos \theta$$

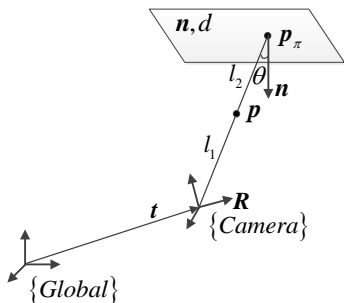
$$\mathbf{n}^T \mathbf{p} + d = l_2 \cos \theta \quad (4)$$

$$\mathbf{n}^T \mathbf{t} + d = l \cos \theta$$

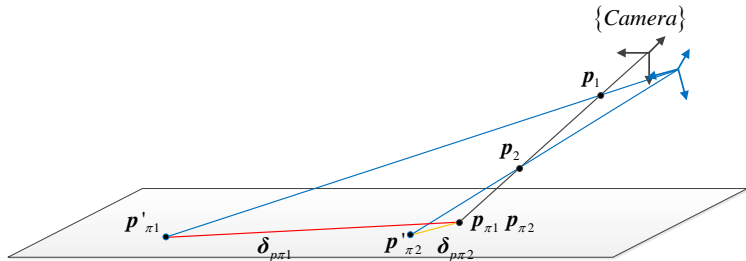
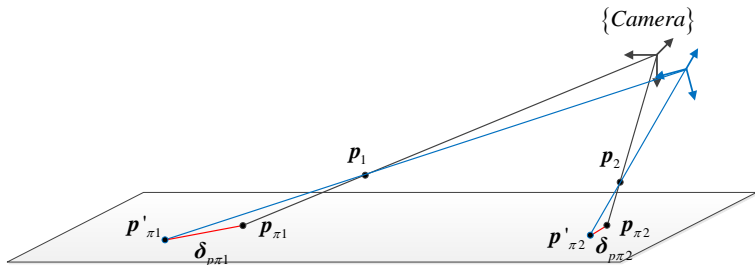
相机运动对Occluded point坐标的影响

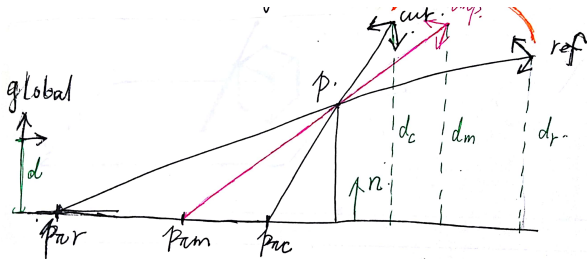
- 代入式(3), Jacobian $\mathbf{J}_{p\pi}$ 可以写为

$$\begin{aligned}\mathbf{J}_{p\pi} &= \begin{bmatrix} \frac{l_2}{l_1^2 \cos \theta} \mathbf{R}^T (\mathbf{t} - \mathbf{p}) \mathbf{n}^T - \frac{l_2}{l_1} \mathbf{R}^T & -\frac{l_2}{l_1} \mathbf{R}^T [\mathbf{t} - \mathbf{p}]_{\times} \end{bmatrix} \\ &= \begin{bmatrix} \frac{l_2}{l_1^2 \cos \theta} \mathbf{R}^T (\mathbf{t} - \mathbf{p}) \mathbf{n}^T & \mathbf{0} \end{bmatrix} - \frac{l_2}{l_1} \mathbf{R}^T [\mathbf{I} \quad [\mathbf{t} - \mathbf{p}]_{\times}] \end{aligned} \quad (5)$$



相机运动对Occluded point坐标的影响

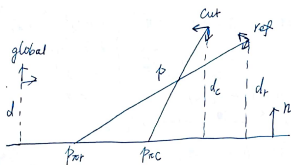




$${}^r p_{pc}^{(2)} = p_{pc} (s=r) = \frac{{}^r n^T t_{rc} + d_r}{n^T (t_{rc} - p)} p + \frac{{}^r n^T p + d_r}{n^T (p - t_{rc})} t_{rc}$$

calculated in $\{ref\}$
 intersection of n plane and ${}^r O_{cur} p$ line.

\downarrow
 $c p_{pc} \Leftrightarrow T_{cr} ({}^r p_{pc}^{(2)})$
 measured in $\{cur\}$.



$$p_{par} = \mu(p, t_{gr}, n, d)$$

$$p_{pac} = \mu(p, t_{gc}, n, d)$$

$$c_p = \text{Toyl}(p) \quad r_p = \text{Toyl}(p)$$

$$c_{p'}^i, r_{p'}^i \left. \begin{array}{l} \\ \\ \\ \end{array} \right\} \text{measurements.}$$

$$c_{p_{par}}^i, r_{p_{par}}^i$$

$$c_{p_{pac}}^i, r_{p_{pac}}^i$$

$$c_{n'}^i, c_{d_c}^i$$

$$r_{n'}^i, r_{d_r}^i$$

$$p_{par} = \mu(p, t_{gr}, n, d)$$

$$p_{pac} = \mu(p, t_{gc}, n, d)$$

$$r_{p_{par}} = \text{Toyl}(p_{par})$$

$$c_{p_{pac}} = \text{Toyl}(p_{pac})$$

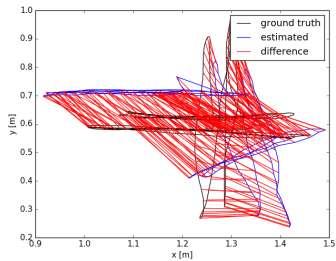
$\text{Toyl} = \{R_{rot}, \text{tor}\}$ — variable.

Constraints:

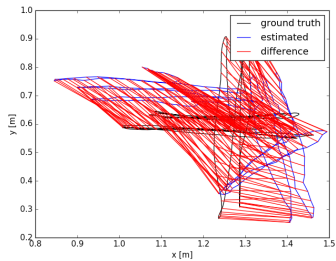
- 1) $c_p^i \leftrightarrow \text{Toyl}(r_{p'}^i) = R_{rot} r_{p'}^i + \text{tor}$
aligning the occluding points (meas.)
- 2) $\begin{bmatrix} c_{n'}^i \\ c_{d_c}^i \end{bmatrix} \leftrightarrow \text{Toyl}^{-T} \begin{bmatrix} r_{n'}^i \\ r_{d_r}^i \end{bmatrix}$ — aligning the planes (meas.)
- 3) $c_{p_{pac}}^i \leftrightarrow$ intersection of the plane (n, d) and the line through p and t_{gc} (described in cut)
- $r_{p_{par}}^i \leftrightarrow$ intersection of the plane (n, d) and the line through p and t_{gr} (described in ref)
- 4) $\left. \begin{array}{l} c_p^i \\ r_{p'}^i \end{array} \right\} \leftrightarrow$ intersection of
 $\left\{ \begin{array}{l} \text{line through } p_{pac} \text{ and } t_{gc} \\ \text{line through } p_{par} \text{ and } t_{gr} \end{array} \right.$

Table:

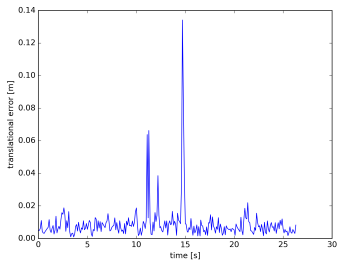
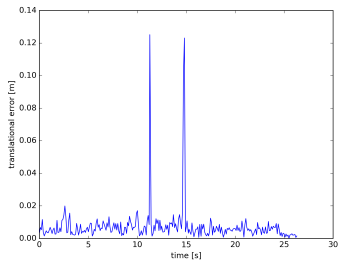
	edge only (ATE)	edge only (RPE)	edge_shadow (ATE)	edge_shadow (RPE)
fr1_xyz	0.169 m	0.014 m/0.708 deg	0.223 m	0.014 m/0.954 deg
fr2_desk	0.065 m	0.003 m/0.336 deg	0.308 m	0.006 m/0.396 deg
fr3_office	0.167 m	0.004 m/0.369 deg	0.372 m	0.019 m/1.142 deg

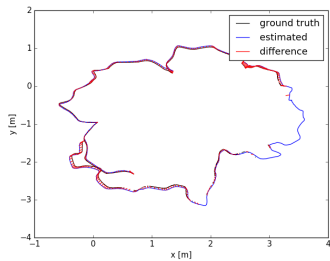


(a) edge only (ATE)

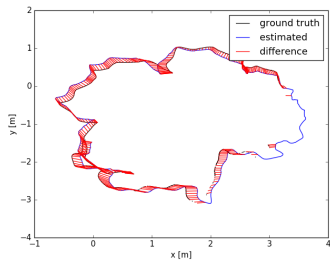


(b) edge_shadow (ATE)

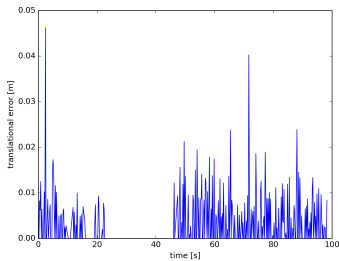
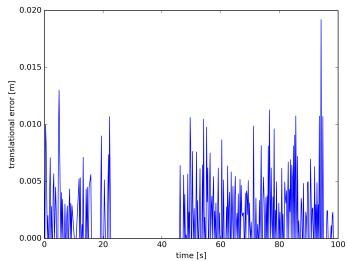


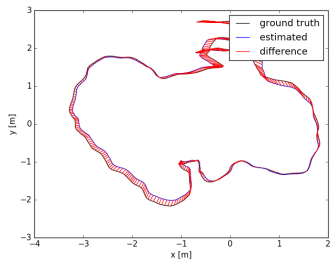


(a) edge only (ATE)

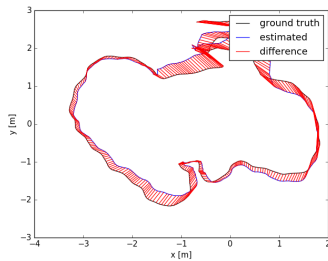


(b) edge_shadow (ATE)





(a) edge only (ATE)



(b) edge_shadow (ATE)

